Partial Volumetric Behavior in Hydrocarbon Systems

Ethane and *n*-Decane in the Liquid Phase of the Ethane–*n*-Decane System

H. H. REAMER, VIRGINIA BERRY, and B. H. SAGE

Chemical Engineering Laboratory, California Institute of Technology, Pasadena, Calif.

PARTIAL MOLAL VOLUMES of the components of binary and multicomponent systems help to determine the heat and work associated with changes in state when used with heat capacity data. They are of particular importance in the evaluation of the molecular transport where the requisite diffusion coefficients are available (3).

Recently, the volumetric and phase behavior of the ethane-*n*-decane system has been investigated (5). These studies were carried out at pressures up to 10,000 p.s.i.a. in the temperature interval between 40° and 460° F. Utilizing these volumetric data, the partial molal volumes of ethane and *n*-decane were evaluated by graphical residual methods whenever feasible.

The partial molal volume (hereafter referred to as partial volume) is defined as

$$\boldsymbol{V}_{k} = \left(\frac{\partial \boldsymbol{V}}{\partial \boldsymbol{m}_{k}}\right)_{T:P:\boldsymbol{m}_{i}}$$
(1)

From the smoothed volumetric data of the ethane-n-decane system (5) in the homogeneous region, large-scale diagrams were prepared of the isobaric-isothermal change in the molal volume composition. The partial volumes of ethane and n-decane at mole fractions greater than 0.4 for each component were determined by the graphical application of the following expression (2):

$$\overline{V}_{k} = V + (1 - n_{k}) \left(\frac{\partial V}{\partial n_{k}} \right)_{T,P}$$
⁽²⁾

Equation 2 loses precision at small mole fractions of the component in question. Therefore, at mole fractions of 0.4 and less for ethane and *n*-decane, the partial volumes were established from

$$\overline{V}_{k} = \frac{V - n_{j} \, \overline{V}_{j}}{n_{k}} \tag{3}$$

The partial volumes of each component were also established from

$$\overline{V}_{k} = V_{k}^{0} - \int_{0}^{1-n_{k}} \left(\frac{n_{j}}{n_{k}}\right) \left(\frac{\partial \overline{V}_{j}}{\partial n_{i}}\right)_{T,P} \mathrm{d}n_{j}$$
(4)

Equation 4 is based upon the Gibbs-Duhem equation (1). The use of Equations 3 and 4 to evaluate the partial volumes at the same state permits a direct check upon the consistency of the calculations.

Table I compares the graphical values determined by Equations 2 and 3 with the integrated values determined by Equation 4 throughout the entire composition interval. The standard error of estimate is recorded for each temperature. An average deviation without regard to sign in the partial volumes for the states (Table I) of 0.8% was found for ethane and 0.14% for *n*-decane. Table I presents typical information encountered throughout the range of pressures, temperatures, and compositions covered in this graphical evaluation of the partial volumes.

Fraction	Eth	nane	n-De	ecane	Eth	nane	n-Decane		
Ethane	Graphical	Integrated	Graphical	Integrated	Graphical	Integrated	Graphical	Integrated	
		5000 P.S	.I.A., 160° F.			10,000	P.S.I.A., 160° I	<i>3</i> .	
0.1	1.099°	1.127	3.143	3.144	1.022	1.047	3.061	3.060	
0.2	1.095	1.108	3.144	3.144	1.013	1.028	3.064	3.063	
0.3	1.090	1.092	3.149	3.147	1.003	1.012	3.069	3.067	
0.4	1.083	1.080	3.155	3.157	0.993	0.999	3.075	3.073	
0.5	1.074	1.072	3.166	3.167	0.984	0.988	3.090	3.083	
0.6	1.072	1.069	3.182	3.182	0.983	0.984	3.100	3.099	
0.7	1.076	1.076	3.163	3.163	0.986	0.989	3.079	3.084	
0.8	1.110	1.112	3.044	3.048	1.005	1.009	3.025	3.028	
0.9	1.172	1.174	2.717	2.701	1.031	1.035	2.875	2.866	
σ^{b}	0	.010		0.006		0.010		0.004	
	5000 P.		5.I.A., 400° F.			10,000	P.S.I.A., 400° I	F.	
0.1	1.384	1.400	3.550	3.550	1.194	1.208	3.372	3.372	
0.2	1.400	1.416	3.549	3.548	1.202	1.209	3.372	3.372	
0.3	1.419	1.432	3.547	3.546	1.211	1.211	3.372	3.371	
0.4	1.445	1.447	3.529	3.530	1.217	1.214	3.366	3.369	
0.5	1.467	1.464	3.512	3.514	1.221	1.218	3.358	3.363	
0.6	1.497	1.486	3.500	3.492	1.228	1.223	3.352	3.355	
0.7	1.536	1.523	3.440	3.442	1.232	1.232	3.340	3.339	
0.8	1.613	1.611	3.182	3.198	1.254	1.254	3.259	3.271	
0.9	1.740	1.737	2.262	2.284	1.290	1.293	2.988	2.981	
σ	0	.010		0.003		0.005		0.005	
Partial molal	volume, cu. ft	./lbmole.							
Standard erro	r of estimate.	cu ft /lb -mole	$\sigma = \left[\sum_{n=1}^{N} \left(\overline{V}\right)\right] =$	$\nabla (1)^2 / N^{1/2}$					

Table I. Internal Consistency of Partial Volumetric Data

The values of the partial volumes of ethane and n-decane are reported in Tables II and III, respectively. These represent smoothed values for even mole fractions of ethane and n-decane. At the lower mole fractions of each of the components, the number of significant figures has been decreased since the uncertainty of evaluation is somewhat larger.

To illustrate the partial volumetric behavior of these two hydrocarbons in the ethane-n-decane system, typical diagrams have been prepared from the tabular data. Figure 1 presents the effect of the mole fraction of ethane upon the partial volume of this component at a temperature of 220° F. For the most part, the behavior is similar to that found for ethane in the ethane-n-pentane system (4). However, at the higher pressures there is a small decrease in the partial volume with an increase in the mole fraction of ethane up to approximately 0.6.

Figure 2 portrays the effect of composition on the partial volume of n-decane at 220° F. At small mole fractions

⁽Continued on page 492)



Figure 1. Influence of composition on the partial molal volume of ethane at 2220° F.

		Table II. P	artial Molal V	olume of Etl	hane in the Et	thane <i>–n</i> -Deco	ane System		
				Mole Fract	tion Ethane				
Pressure,									
P.S.I.A.	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
				40	° F.				
	$(40)^{a}$	(81)	(118)	(155)	(190)	(230)	(270)	(310)	(350)
Bubble Point	1.08°	1.07	1.053	1.042	1.041	1.053	1.078	1.113	1.153
200	1.08^{b}	1.06	1.051	1.040	1.040		• • • •		
400	1.07	1.06	1.047	1.035	1.031	1.047	1.072	1.108	1.149
600	1.07	1.06	1.043	1.030	1.024	1.040	1.065	1.097	1.132
800	1.06	1.05	1.039	1.025	1.018	1.034	1.057	1.085	1.118
1,000	1.06	1.04	1.035	1.021	1.012	1.028	1.050	1.075	1.105
1,250	1.05	1.04	1.031	1.017	1.006	1.021	1.042	1.064	1.090
1,500	1.04	1.03	1.025	1.012	1.001	1.014	1.033	1.055	1.078
1,750	1.03	1.03	1.021	1.008	0.997	1.008	1.026	1.046	1.068
2,000	1.03	1.02	1.017	1.004	0.994	1.002	1.020	1.039	1.059
2,250	1.02	1.02	1.011	1.000	0.990	0.997	1.013	1.032	1.050
2,500	1.02	1.01	1.008	0.997	0.987	0.992	1.007	1.025	1.043
2,750	1.01	1.01	1.004	0.994	0.983	0.987	1.001	1.018	1.036
3,000	1.00	1.00	0.999	0.990	0.980	0.983	0.996	1.012	1.030
3,500	1.00	0.99	0.991	0.984	0.973	0.975	0.987	1.001	1.017
4,000	0.99	0.99	0.982	0.976	0.967	0.967	0.978	0.991	1.008
4,500	0.98	0.98	0.975	0.969	0.960	0.960	0.970	0.982	0.999
5,000	0.97	0.97	0.968	0.962	0.954	0.953	0.962	0.973	0.990
6,000	0.96	0.96	0.955	0.950	0.943	0.940	0.946	0.957	0.974
7,000	0.95	0.95	0.943	0.938	0.932	0.929	0.933	0.943	0.960
8,000	0.94	0.94	0.933	0.928	0.923	0.919	0.922	0.931	0.947
9,000	0.93	0.93	0.925	0.920	0.915	0.910	0.912	0.919	0.934
10,000	0.92	0.92	0.916	0.912	0.908	0.903	0.904	0.910	0.925
	(05)((****	(* • • • •)	10	00° F.				
	(65)°	(130)	(197)	(265)	(338)	(417)	(497)	(586)	(681)
	1.15°	1.14	1.140	1.137	1.135	1.141	1.178	1.266	1.442
200	1.14^b	1.14	1.139						
400	1.14	1.14	1.132	1.131	1.131				
600	1.13	1.13	1.126	1.123	1.122	1.128	1.164	1.262	
800	1.12	1.12	1.119	1.115	1.112	1.116	1.145	1.235	1.397
1,000	1.12	1.12	1.113	1.108	1.104	1.107	1.133	1.210	1.345
1,250	1.11	1.11	1.105	1.099	1.095	1.097	1.120	1.184	1.300
1,500	1.10	1.10	1.098	1.092	1.087	1.089	1.108	1.164	1.264
1,750	1.10	1.10	1.092	1.085	1.079	1.080	1.098	1.149	1.235
2,000	1.09	1.09	1.086	1.078	1.072	1.073	1.088	1.136	1.212
2,250	1.09	1.08	1.080	1.072	1.065	1.065	1.080	1.125	1.192
2,500	1.08	1.08	1.074	1.066	1.059	1.058	1.073	1.114	1.175
2,750	1.08	1.07	1.069	1.061	1.053	1.052	1.066	1.104	1.160
3,000	1.07	1.07	1.064	1.055	1.047	1.046	1.060	1.095	1.147
3,500	1.06	1.06	1.056	1.045	1.036	1.035	1.048	1.076	1.124
4,000	1.05	1.05	1.045	1.035	1.027	1.026	1.037	1.058	1.104
4,500	1.04	1.04	1.036	1.025	1.016	1.015	1.026	1.044	1.088
5,000	1.03	1.03	1.027	1.015	1.006	1.006	1.015	1.032	1.075
6,000	1.02	1.02	1.010	0.998	0.990	0.989	0.995	1.011	1.049
7,000	1.01	1.00	0.995	0.984	0.975	0.974	0.978	0.994	1.027
8,000	1.00	0.99	0.980	0.971	0.963	0.959	0.963	0.978	1.008
9,000	0.98	0.98	0.968	0.960	0.952	0.947	0.949	0.964	0.990
10,000	0.97	0.96	0.958	0.950	0.942	0.936	0.938	0.954	0.974

Table II. Partial Molal Volume of Ethane in the Ethane–n-Decane System

Pressure, P.S.I.A.	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
				16	0° F.				
Bubble Point	$(91)^a$ 1.23^b	(186) 1.24	(287) 1.243	(394) 1.252	(511) 1.265	(639) 1.286	(783) 1.338	(940) 1.494	(1112) 1.928
$\begin{array}{c} 200\\ 400\\ 600\\ 800\\ 1,000\\ 1,250\\ 1,500\\ 1,750\\ 2,000\\ 2,250\\ 2,500\\ 2,500\\ 2,500\\ 2,500\\ 3,500\\ 4,000\\ 4,500\\ 5,000\\ 6,000\\ 7,000\\ 8,000\\ 9,000\\ \end{array}$	1.23° 1.23° 1.22 1.21 1.20 1.19 1.18 1.18 1.18 1.18 1.17 1.16 1.16 1.15 1.14 1.13 1.12 1.11 1.10 1.08 1.06 1.05 1.04	$1.24 \\ 1.23 \\ 1.22 \\ 1.21 \\ 1.20 \\ 1.20 \\ 1.19 \\ 1.18 \\ 1.17 \\ 1.16 \\ 1.16 \\ 1.16 \\ 1.15 \\ 1.14 \\ 1.13 \\ 1.12 \\ 1.11 \\ 1.10 \\ 1.07 \\ 1.06 \\ 1.04 \\ 1.03 \\ 1.03 \\ 1.02 \\ 1.03 \\ 1.02 \\ 1.02 \\ 1.04 \\ 1.03 \\ 1.02 \\ 1.02 \\ 1.02 \\ 1.02 \\ 1.02 \\ 1.02 \\ 1.03 \\ 1.02 \\ 1.02 \\ 1.03 \\ 1.03 \\ 1.02 \\ 1.03 \\ 1.03 \\ 1.02 \\ 1.03 \\ 1.02 \\ 1.03 \\ 1.02 \\ 1.03 \\ 1.03 \\ 1.02 \\ 1.03 \\ 1.02 \\ 1.03 \\ 1.03 \\ 1.02 \\ 1.03 \\ 1.03 \\ 1.02 \\ 1.03 \\ $	$\begin{array}{c} 1.237\\ 1.228\\ 1.219\\ 1.211\\ 1.201\\ 1.192\\ 1.182\\ 1.174\\ 1.165\\ 1.156\\ 1.149\\ 1.141\\ 1.127\\ 1.114\\ 1.102\\ 1.090\\ 1.049\\ 1.049\\ 1.032\\ 1.016\\ \end{array}$	$\begin{array}{c} 1.252\\ 1.241\\ 1.230\\ 1.208\\ 1.197\\ 1.186\\ 1.172\\ 1.166\\ 1.156\\ 1.147\\ 1.138\\ 1.123\\ 1.110\\ 1.096\\ 1.083\\ 1.060\\ 1.038\\ 1.022\\ 1.006\\ \end{array}$	$\begin{array}{c} \dots \\ 1.259 \\ 1.245 \\ 1.232 \\ 1.217 \\ 1.204 \\ 1.191 \\ 1.180 \\ 1.168 \\ 1.157 \\ 1.146 \\ 1.136 \\ 1.118 \\ 1.102 \\ 1.087 \\ 1.074 \\ 1.049 \\ 1.028 \\ 1.011 \\ 0.996 \end{array}$	$\begin{array}{c} \dots \\ \dots \\ 1.272 \\ 1.256 \\ 1.237 \\ 1.219 \\ 1.202 \\ 1.186 \\ 1.173 \\ 1.161 \\ 1.150 \\ 1.138 \\ 1.120 \\ 1.086 \\ 1.072 \\ 1.086 \\ 1.072 \\ 1.047 \\ 1.022 \\ 1.047 \\ 1.022 \\ 1.010 \\ 0.995 \end{array}$	1.000 1.332 1.297 1.268 1.244 1.223 1.204 1.187 1.173 1.159 1.147 1.126 1.107 1.091 1.076 1.032 1.015 0.999	$\begin{array}{c} \dots \\ \dots \\ \dots \\ 1.478 \\ 1.419 \\ 1.370 \\ 1.332 \\ 1.300 \\ 1.273 \\ 1.250 \\ 1.229 \\ 1.210 \\ 1.128 \\ 1.110 \\ 1.080 \\ 1.057 \\ 1.038 \\ 1.020 \end{array}$	$\begin{array}{c} \dots \\ \dots $
10,000	1.02	1.01	1.003	0.993	0.984	0.983	0.986	1.005	1.031
	$(117)^{a}$	(244)	(380)	22 (526)	0° F. (692)	(876)	(1080)	(1299)	(1502)
Bubble Point $\begin{array}{c} 200\\ 400\\ 600\\ 800\\ 1,000\\ 2,250\\ 1,500\\ 1,750\\ 2,000\\ 2,250\\ 2,500\\ 2,500\\ 2,500\\ 2,500\\ 2,750\\ 3,000\\ 3,500\\ 4,000\\ 4,500\\ 5,000\\ 6,000\\ 7,000\\ 8,000\\ 9,000\\ 10,000\\ \end{array}$	$\begin{array}{c} 1.36^\circ\\ 1.35^\circ\\ 1.34\\ 1.33\\ 1.31\\ 1.30\\ 1.29\\ 1.28\\ 1.27\\ 1.26\\ 1.25\\ 1.24\\ 1.23\\ 1.22\\ 1.20\\ 1.19\\ 1.17\\ 1.16\\ 1.14\\ 1.12\\ 1.10\\ 1.08\\ 1.07\\ \end{array}$	$\begin{array}{c} 1.37\\ 1.36\\ 1.35\\ 1.34\\ 1.32\\ 1.31\\ 1.30\\ 1.28\\ 1.27\\ 1.26\\ 1.25\\ 1.23\\ 1.22\\ 1.20\\ 1.19\\ 1.17\\ 1.16\\ 1.13\\ 1.11\\ 1.09\\ 1.08\\ 1.06\\ \end{array}$	$\begin{array}{c} 1.385\\ 1.368\\ 1.368\\ 1.356\\ 1.344\\ 1.328\\ 1.312\\ 1.298\\ 1.284\\ 1.269\\ 1.254\\ 1.241\\ 1.228\\ 1.205\\ 1.186\\ 1.169\\ 1.154\\ 1.128\\ 1.102\\ 1.084\\ 1.068\\ 1.054\\ \end{array}$	$\begin{array}{c} 1.408 \\ \hline \\ 1.400 \\ 1.383 \\ 1.368 \\ 1.349 \\ 1.332 \\ 1.314 \\ 1.298 \\ 1.281 \\ 1.264 \\ 1.249 \\ 1.233 \\ 1.208 \\ 1.189 \\ 1.169 \\ 1.152 \\ 1.121 \\ 1.095 \\ 1.076 \\ 1.060 \\ 1.045 \end{array}$	1.442 $$ 1.422 1.397 1.374 1.354 1.332 1.312 1.292 1.272 1.254 1.238 1.211 1.190 1.169 1.169 1.150 1.115 1.091 1.068 1.052 1.038	1.504 $$ 1.475 1.475 1.430 1.391 1.358 1.327 1.300 1.280 1.260 1.243 1.212 1.190 1.166 1.148 1.112 1.086 1.064 1.048 1.036	$\begin{array}{c} 1.618\\ \dots\\ 1.618\\ \dots\\ 1.564\\ 1.496\\ 1.439\\ 1.392\\ 1.351\\ 1.318\\ 1.290\\ 1.266\\ 1.231\\ 1.203\\ 1.179\\ 1.158\\ 1.123\\ 1.096\\ 1.073\\ 1.056\\ 1.043\\ \end{array}$	$\begin{array}{c} 1.908\\ \dots\\ \dots\\$	2.726 2.096 1.883 1.744 1.650 1.524 1.439 1.375 1.327 1.288 1.228 1.128 1.148 1.148 1.120 1.094
	(147)0	(201)	(460)	2	80° F.	(1109)	(1961)	(1596)	(1680)
Bubble Point 200 400 600 800 1,000 1,250 1,750 2,000 2,250 2,500 2,750 3,000 3,500 4,000 4,500 5,000 6,000 7,000 8,000 9,000 10,000	1.53° 1.52° 1.50 1.48 1.46 1.44 1.42 1.40 1.38 1.36 1.34 1.33 1.30 1.28 1.25 1.24 1.22 1.19 1.15 1.12 1.11	1.55 1.53 1.51 1.48 1.46 1.44 1.42 1.40 1.38 1.36 1.34 1.32 1.31 1.28 1.26 1.24 1.22 1.20 1.17 1.14 1.12	1.566 1.546 1.520 1.495 1.467 1.441 1.417 1.395 1.375 1.356 1.339 1.323 1.295 1.271 1.250 1.231 1.199 1.169 1.143 1.121 1.105	1.597 1.597 1.573 1.573 1.501 1.469 1.441 1.416 1.394 1.372 1.353 1.305 1.281 1.258 1.281 1.258 1.281 1.258 1.236 1.198 1.168 1.141 1.120 1.104	1.651 1.623 1.568 1.522 1.485 1.452 1.423 1.397 1.373 1.350 1.317 1.290 1.265 1.240 1.199 1.166 1.140 1.118 1.102	1.760 1.760 1.718 1.652 1.588 1.528 1.477 1.437 1.437 1.404 1.377 1.338 1.304 1.274 1.247 1.200 1.163 1.136 1.115 1.099	2.021 1.950 1.820 1.682 1.593 1.528 1.479 1.443 1.382 1.336 1.298 1.298 1.265 1.212 1.170 1.146 1.126 1.08	2.658 2.658 2.658 2.277 2.020 1.855 1.744 1.662 1.591 1.488 1.414 1.358 1.315 1.251 1.204 1.171 1.145 1.126	$\begin{array}{c} \dots \\ \dots $

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1,250 1.80 1.87 1.974 2.212 2.820	
1,500 1.75 1.80 1.882 2.045 2.366 3.219 1.750 1.751 1.75 1.811 1.923 2.112 2.512 2.307 4.106	467
2.000 1.67 1.70 1.752 1.835 1.970 2.269 2.793 3.396	.407
2,250 1.63 1.66 1.705 1.771 1.885 2.118 2.509 2.993 3	.390
2,500 1.60 1.63 1.663 1.721 1.819 1.999 2.293 2.666 3	.020
3,000 1.57 1.56 1.596 1.673 1.704 1.907 2.152 2.406 2 3,000 1.54 1.56 1.596 1.643 1.717 1.832 2.007 2.218	.724 463
3,500 1.49 1.51 1.541 1.580 1.637 1.714 1.824 1.976	.184
4,000 1.45 1.47 1.491 1.527 1.570 1.624 1.697 1.814 1	.997
4,500 1.42 1.43 1.453 1.480 1.514 1.554 1.607 1.700 1 5000 1.38 1.40 1.419 1.441 1.467 1.497 1.592 1.612 1	.852
6,000 1.30 1.40 1.410 1.441 1.407 1.497 1.500 1.013 1 6,000 1.32 1.34 1.363 1.375 1.392 1.410 1.434 1.485 1	.740 583
7,000 1.28 1.30 1.312 1.325 1.334 1.348 1.363 1.394 1	.475
8,000 1.24 1.26 1.275 1.284 1.290 1.300 1.309 1.334 1 9,000 1.92 1.92 1.941 1.940 1.955 1.959 1.959 1.959	.396
10,000 1.22 1.23 1.241 1.249 1.255 1.263 1.269 1.290 1 $10,000$ 1.19 1.20 1.211 1.217 1.221 1.228 1.232 1.254 1	.336
460° F.	
$(274)^a$ (490) (710) (943) (1193) (1410) (1477) (1363) ()
Bubble Point 2.45^b 2.86 3.680 6.020 \dots \dots \dots	
200	• • •
400 2.37°	• • •
$800 2.25 2.70 \dots \dots$	• • •
1,000 2.11 2.31 2.760 4.520	
1,250 2.04 2.18 2.438 3.104 4.724	
1,500 1.97 2.09 2.273 2.650 3.360 4.410 5.780 1.750 1.750 1.90 2.00 2.156 2.410 2.927 3.420 4.927 4.927	
2,000 1.86 2.06 2.165 2.415 2.667 3.430 4.225 4.822 2 2.000 1.84 1.93 2.060 2.271 2.576 2.954 3.471 4.139 2	.030
2,250 1.79 1.87 1.977 2.150 2.383 2.651 3.012 3.572	.878
2,500 1.74 1.81 1.905 2.034 2.207 2.426 2.721 3.168 3	.476
2,700 1.70 1.643 1.950 2.086 2.247 2.476 2.835 3 3.000 1.66 1.72 1.788 1.877 1.987 2.118 2.208 2.600 c	.134
3,500 1.60 1.65 1.698 1.761 1.838 1.929 2.055 2.266 2	.466
4,000 1.55 1.59 1.626 1.673 1.730 1.792 1.890 2.050 2	.219
4,000 1.00 1.00 1.067 1.607 1.650 1.696 1.765 1.899 2 5.000 1.46 1.48 1.518 1.559 1.588 1.692 1.699 1.704 $-$.044
6,000 1.39 1.41 1.441 1.467 1.494 1.518 1.518 1.546 1.615 1	.309 .709
$7,000 \qquad 1.33 \qquad 1.36 \qquad 1.381 \qquad 1.402 \qquad 1.421 \qquad 1.440 \qquad 1.467 \qquad 1.503 \qquad 1$.576
8,000 1.28 1.31 1.329 1.345 1.361 1.376 1.393 1.422 1 9.000 1.25 1.26 1.280 1.293 1.206 1.200 1.200 1.200	.479
10,000 1.22 1.23 1.207 1.247 1.259 1.300	.360

 $^{\rm a}$ Values in parentheses represent bubble-point pressures in p.s.i. $^{\rm b}$ Partial molal volumes are in cu. ft./lb.-mole.

Mole Fraction *n*-Decane 40° F.

Pressure, P.S.I.A.	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
	(350)°	(310)	(270)	(230)	(190)	(155)	(118)	(81)	(40)
Bubble Point	2.51^{b}	2.88	2.996	3.046	3.070	3.073	3.067	3.059	3.056
200	2.60*	2.89	2 999	3 044	3.069	3.072	3.064	3.056	3.052
4 00 6 00	2.60	2.90	3.002	3.045	3.065	3.063	3.056	3.048	3.045
800	2.68	2.92	3.003	3.044	3.061	3.058	3.051	3.043	3.041
1,000	2.72	2.93	3.004	3.042	3.057	3.054	3.047	3.039	3.038
1,250	2.76	2.94	3.004	3.039	3.054	3.049	3.042	3.034	3.033
1,500	2.79	2.95	3.004	3.035	3.048	3.044	3.037	3.025	3.029
2,000	2.82	2.95	3.002	3.028	3.036	3.033	3.026	3.021	3.020
2,250	2.82	2.95	3.000	3.024	3.030	3.077	3.022	3.017	3.015
2,500	2.81	2.95	2.997	3.020	3.025	3.022	3.016 3.011	3.012 3.007	3.011
3.000	2.80	2.94 2.94	2.991	3.013	3.017	3.012	3.007	3.004	3.003
3,500	2.79	2.94	2.986	3.007	3.009	3.004	3.000	2.997	2.995
4,000	2.78	2.94	2.982	3.000	3.001	2.996	2.992	2.990	2.988
4,500	2.77	2.94	2.978	2.994	2.994	2.989	2.985	2.982	2.980
6,000	2.76	2.92	2.967	2.977	2.975	2.970	2.965	2.963	2.961
7,000	2.76	2.92	2.958	2.966	2.963	2.957	2.953	2.951	2.950
8,000	2.75	2.91	2.950	2.956	2.951	2.946	2.942	2.940	2.939
9,000	2.73 2.74	2.89	2.942	2.946	2.941	2.928	2.924	2.930	2.930
10,000				10	00° F.				
	(681) ^a	(586)	(497)	(417)	(338)	(265)	(197)	(130)	(65)
Bubble Point	1.66°	2.83	3.050	3.138	3.162	3.165	3.166	3.166	3.166
200		• • •	• • •		2 169	2 161	3.166	3.163	3.161
400 600		2.83	3.068	3.156	3.162	3.156	3.159	3.150	3.134
800	1.76*	2.86	3.097	3.166	3.159	3.151	3.147	3.144	3.143
1,000	1.98	2.88	3.116	3.166	3.153	3.146	3.142	3.138	3.137
1,250 1,500	2.16	2.91	3.128 3.128	3.162 3.157	3.147 3.141	3.139	3,136	3.132	3.130
1,750	2.29	2.95	3.128 3.122	3.151	3.135	3.127	3.124	3.120	3.117
2,000	2.47	2.96	3.117	3.145	3.130	3.121	3.117	3.114	3.112
2,250	2.53	2.97	3.112	3.139	3.125	3.116	3.112	3.109	3.107
2,500	2.58	2.97	3.107	3.132 3.124	3.120	$3.111 \\ 3.107$	3.106	3.098	3.102
3,000	2.61	2.98	3.098	3.117	3.110	3.102	3.096	3.093	3.092
3,500	2.68	2.99	2.090	3.105	3.101	3.094	3.086	3.083	3.082
4,000	2.72	2.99	3.082	3.095	3.093	3.086	3.078	3.074	3.073
5.000	2.74	2.99	3.068	3.079	3.076	3.070	3.061	3.057	3.056
6,000	2.78	2.98	3.055	3.067	3.063	3.055	3.046	3.043	3.042
7,000	2.79	2.97	3.044	3.056	3.051	3.041	3.032	3.029	3.028
8,000	2.80	2.97	3.033	3.044	3.039	3.029	3.007	3.003	3.015
10,000	2.82	2.97	3.007	3.019	3.014	3.004	2.995	2,992	2.991
,				16	60° F.				
	$(1112)^{a}$	(940)	(783)	(639)	(511)	(394)	(287)	(186)	(91)
Bubble Point	• • •	2.50	3.046	3.209	3.253	3.266	3.275	3,283	3.287
200		• • •		• • •		2 265	2 971	3.282	3.287
400			• • •	• • •	3.251	3.265	3.265	3.274 3.265	3.265
800			3.090	3.213	3.248	3.260	3.258	3.257	3.257
1,000		2.54	3.141	3.217	3.244	3.254	3.251	3.248	3.248
1,250 1,500	0.65°	2.69	$3.165 \\ 3.178$	3.219	3.239	3.247	$3.244 \\ 3.237$	3.240	3.240
1,500	$1.20 \\ 1.64$	2.83	3.185	3.220	3.229	3.233	3.230	3.225	3.224
2,000	1.85	2.87	3.189	3.219	3.224	3.226	3.222	3.218	3.217
2,250	2.02	2.91	3.191	3.217	3.219	3.220	3.215 3.209	3.211	3.210
2,500 2,750	2.17	2.94 2.96	3,189	3.211	3.208	3.207	3.202	3.198	3.196
3,000	2.40	2.98	3.187	3.208	3.203	3.201	$3.19\overline{6}$	3.191	3.188
3,500	2.53	3.01	3.183	3.200	3.193	3.188	3.184	3.178	3.176
4,000 4,500	2.62	3.03 3.04	3.177 3.171	3.192 3.183	3.183 3.174	3.1 <i>11</i> 3.167	3.162	3.157	3.164
5,000	2.72	3.04	3.163	3.174	3.166	3.159	3.152	3.147	3.143
6,000	2.78	3.04	3.145	3.157	3.150	3.142	3.134	3.128	3.123
7,000	2.82	3.04	$3.128 \\ 3.111$	3.142 3.198	3.136 3.191	3.127 3.119	3.117 3.101	3.110	3.106
9.000	2.83 2.87	3.03	3.095	3.112	3.105	3.096	3.086	3.077	3.073
10,000	2.88	3.02	3.079	3.097	3.090	3.081	3.071	3.063	3.059

Table III. Partial Molal Volume of n-Decane in the Ethane-n-Decane System

Pressure, P.S.I.A.	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
				25	20° F.				
Bubble Point	(1502) ^a	(1299) 1.84	1080) 2.913	(876) 3.251	(692) 3.336	$(526) \\ 3.368$	(380) 3.388	(244) 3.406	$(117) \\ 3.426$
$\begin{array}{c} 200\\ 400\\ 600\\ 800\\ 1,000\\ 1,250\\ 1,500\\ 1,750\\ 2,000\\ 2,250\\ 2,500\\ 2,750\\ 3,000\\ 3,500\\ 4,000 \end{array}$	$\begin{array}{c} \cdots \\ 0.74 \\ 1.34 \\ 1.68 \\ 1.92 \\ 2.08 \\ 2.34 \\ 2.48 \end{array}$	 2.12 2.41 2.60 2.72 2.79 2.85 2.90 2.99 3.04	2.975 3.056 3.124 3.173 3.209 3.235 3.252 3.263 3.263 3.263	 3.257 3.268 3.278 3.287 3.295 3.302 3.307 3.310 3.310 3.310 3.310 3.305 3.293	 3.335 3.333 3.326 3.322 3.317 3.312 3.306 3.300 3.294 3.282 3.270	$\begin{array}{c} 3.366\\ 3.360\\ 3.353\\ 3.346\\ 3.338\\ 3.330\\ 3.323\\ 3.315\\ 3.307\\ 3.300\\ 3.294\\ 3.280\\ 3.268\end{array}$	3.387 3.376 3.366 3.358 3.349 3.340 3.332 3.324 3.316 3.308 3.308 3.300 3.294 3.280 3.285	3.397 3.385 3.374 3.364 3.353 3.343 3.325 3.317 3.309 3.301 3.294 3.280 3.265	3.418 3.400 3.386 3.375 3.365 3.353 3.344 3.335 3.326 3.318 3.302 3.294 3.280 3.281 3.281 3.281 3.281 3.281 3.282 3.284 3.285 3.284 3.285 3.284 3.285 3.284 3.285 3.284 3.285 3.284 3.285 3
4,500 5,000 6,000 7,000 8,000 9,000 10,000	$2.57 \\ 2.65 \\ 2.76 \\ 2.83 \\ 2.87 \\ 2.89 \\ 2.90 $	3.08 3.09 3.10 3.09 3.09 3.09 3.08 3.07	3.249 3.240 3.221 3.203 3.185 3.167 3.150	3.280 3.267 3.245 3.225 3.206 3.187 3.169	3.260 3.251 3.233 3.215 3.196 3.178 3.160	3.254 3.242 3.222 3.206 3.187 3.168 3.148	3.251 3.238 3.219 3.199 3.178 3.158 3.138	3.251 3.238 3.215 3.193 3.171 3.150 3.130	$\begin{array}{c} 3.251 \\ 3.238 \\ 3.214 \\ 3.192 \\ 3.168 \\ 3.148 \\ 3.128 \end{array}$
				28	0° F.				
Bubble Point	(1680)°	(1596) 0.56	(1361) 2 400	(1102) 3 201	(870) 3.415	(661) 3 490	(469) 3 519	(301) 3 546	(147)
$\begin{array}{c} 200\\ 400\\ 600\\ 800\\ 1,000\\ 1,250\\ 1,500\\ 1,750\\ 2,000\\ 2,250\\ 2,500\\ 2,750\\ 3,000\\ 3,500\\ 4,000\\ 4,500\\ 5,000\\ 6,000\\ 7,000\\ 8,000\\ 9,000\\ 10,000\\ \end{array}$	$\begin{array}{c} & & & \\$	$\begin{array}{c} \dots \\ \dots $	2.100 2.558 2.820 3.020 3.136 3.215 3.252 3.272 3.297 3.310 3.314 3.313 3.300 3.282 3.260 3.237 3.215	3.221 3.253 3.287 3.320 3.349 3.368 3.378 3.368 3.378 3.368 3.378 3.366 3.350 3.338 3.328 3.328 3.3291 3.291 3.270 3.224	$\begin{array}{c}\\\\ 3.417\\ 3.421\\ 3.422\\ 3.422\\ 3.422\\ 3.420\\ 3.414\\ 3.406\\ 3.396\\ 3.387\\ 3.370\\ 3.354\\ 3.341\\ 3.330\\ 3.354\\ 3.341\\ 3.330\\ 3.312\\ 3.293\\ 3.272\\ 3.248\\ 3.224\\ \end{array}$	3.479 3.466 3.454 3.443 3.443 3.434 3.425 3.416 3.407 3.398 3.389 3.372 3.357 3.343 3.330 3.308 3.288 3.265 3.241 3.216	$\begin{array}{c} 3.509\\ 3.496\\ 3.483\\ 3.469\\ 3.456\\ 3.444\\ 3.434\\ 3.424\\ 3.414\\ 3.405\\ 3.396\\ 3.379\\ 3.364\\ 3.349\\ 3.335\\ 3.306\\ 3.278\\ 3.228\\ 3.204\\ \end{array}$	3.340 3.536 3.520 3.609 3.492 3.477 3.464 3.452 3.441 3.430 3.420 3.420 3.410 3.420 3.410 3.420 3.410 3.367 3.351 3.335 3.306 3.276 3.224 3.201	3.567 3.557 3.538 3.509 3.496 3.482 3.468 3.444 3.434 3.424 3.424 3.414 3.424 3.424 3.388 3.370 3.352 3.335 3.306 3.276 3.220 3.224 3.201
	(1051)%		(1505)	34	0° F.	/	<i>(</i>)		
Bubble Point	(1651)	(1707) -1.00	(1535) 1.710	(1286) 2.884	(1018) 3.362	3.593	(552) 3.664	(361) 3.701	(178) 3.723
$\begin{array}{c} 200\\ 400\\ 600\\ 800\\ 1,000\\ 1,250\\ 1,500\\ 2,250\\ 2,500\\ 2,750\\ 3,000\\ 3,500\\ 4,000\\ 4,500\\ 5,000\\ 6,000\\ 7,000\\ 8,000\\ 9,000\\ 10,000\\ \end{array}$	$\begin{array}{c} \cdots \\ \cdots \\ -3.16^{\circ} \\ -1.93 \\ -0.64 \\ 0.19 \\ 0.83 \\ 1.28 \\ 1.75 \\ 2.03 \\ 2.24 \\ 2.40 \\ 2.63 \\ 2.77 \\ 2.85 \\ 2.90 \\ 2.94 \end{array}$	$\begin{array}{c} \dots \\ \dots $	$\begin{array}{c} \dots \\ \dots $	$\begin{array}{c} \dots \\ \dots $	$\begin{array}{c} \dots \\ \dots \\ 3.478 \\ 3.512 \\ 3.518 \\ 3.517 \\ 3.513 \\ 3.506 \\ 3.498 \\ 3.488 \\ 3.466 \\ 3.445 \\ 3.428 \\ 3.414 \\ 3.392 \\ 3.371 \\ 3.344 \\ 3.315 \\ 3.286 \end{array}$	$\begin{array}{c} \dots \\ 3.602 \\ 3.603 \\ 3.596 \\ 3.585 \\ 3.574 \\ 3.562 \\ 3.548 \\ 3.534 \\ 3.520 \\ 3.507 \\ 3.483 \\ 3.461 \\ 3.442 \\ 3.425 \\ 3.394 \\ 3.368 \\ 3.341 \\ 3.312 \\ 3.285 \end{array}$	$\begin{array}{c} \\ 3.661 \\ 3.647 \\ 3.633 \\ 3.617 \\ 3.601 \\ 3.585 \\ 3.570 \\ 3.556 \\ 3.552 \\ 3.515 \\ 3.542 \\ 3.515 \\ 3.492 \\ 3.471 \\ 3.450 \\ 3.431 \\ 3.396 \\ 3.363 \\ 3.334 \\ 3.308 \\ 3.284 \end{array}$	3.695 3.676 3.629 3.643 3.624 3.607 3.590 3.575 3.561 3.548 3.523 3.499 3.477 3.435 3.435 3.398 3.308 3.283	3.719 3.699 3.679 3.646 3.627 3.610 3.579 3.579 3.564 3.552 3.552 3.542 3.525 3.482 3.4461 3.439 3.401 3.335 3.335 3.335 3.307 3.281

Table III. Partial Molal Volume of n-Decane in the Ethane-n-Decane System

Pressure,									
P.S.I.A.	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
				40	0° F.				
	(1497) ^a	(1634)	(1605)	(1391)	(1124)	(865)	(633)	(424)	(222)
Bubble Point			0.560	1.966	3.054	3.502	3.746	3.860	3.925
200									
400					•••		• • •		3.895
600	• • •	· • •	• • •		• • •	• • •	0.745	3.835	3.867
800	•••	• • •	• • •		•••	2 5 40	3.745	3.813	3.842
1,000	• • •	• • •	• • •			3.042	0.744	0.790	3.620
1,200	•••		• • •	2 426	3.100	3.610	3.736	3 751	3.754
1,500	-2.80°	-0.93	1.557	2.420	3 500	3.676	3 722	3 732	3 747
2,000	-2.00	-0.18	2.202	3.106	3.560	3.684	3.706	3.714	3.727
2.250	-1.03	1.06	2.590	3.290	3.576	3.676	3.690	3.697	3.707
2,500	-0.33	1.71	2.842	3.346	3.581	3.663	3.674	3.682	3.689
2,750	0.48	2.19	3.022	3.392	3.582	3.648	3.659	3.666	3.672
3,000	1.05	2.48	3.144	3.430	3.579	3.631	3.644	3.651	3.657
3,500	1.53	2.79	3.290	3.476	3.565	3.602	3.616	3.622	3.628
4,000	1.84	2.97	3.370	3.500	3.547	3.576	3.590	3.596	3.600
4,500	2.07	3.10	3.416	3.506	3.529	3.552	3.568	3.572	3.573
5,000	2.26	3.18	3.440	3.500	3.512	3.529	3,047	3.549	3.000
7,000	2.00	0.20 3.31	3.440	3.472	3.400	3,451	3 466	3 468	3 469
8,000	2.10	2 21	3 396	3 4 1 9	3 418	3 426	3 433	3 433	3 4 3 3
9,000	2.00	3 29	3.367	3.382	3.387	3.395	3.400	3.400	3.400
10.000	2.99	3.26	3.340	3.352	3.358	3.366	3.372	3.372	3.372
- ,				46	0° F				
	()	(1969)	(1477)	(1410)	(1102)	(042)	(710)	(400)	(974)
Bubble Point	(\ldots)	(1303)	(1477)	(1410) 0.200	(1193)	943) 9949	3 545	3 923	4 1 2 0
Bubble Folint	• • •	• • •	• • •	0.200	1.500	2.345	0.040	0.020	4.120
200		• • •			• • •	• • •	• • •		
400	• • •	• • •	• • •		• • •	• • •		2 000	4.120
800	• • •	•••	• • •	• • •	• • •		3 684	4 010	4.100
1 000			• • •		• • •	3.166	3.834	4.007	4.034
1,250					2.500	3.472	3.865	3.984	3.996
1,500			-0.587	2.100	3.085	3.600	3.865	3.954	3.961
1,750	-1.60°	0.45	1.132	2.650	3.350	3.682	3.858	3.920	3.929
2,000	-1.08	0.19	1.960	2.994	3.483	3.730	3.844	3.890	3.899
2,250	-0.55	0.79	2.480	3.182	3.554	3.750	3.828	3.860	3.872
2,500	-0.06	1.44	2.766	3.302	3.600	3.756	3.808	3.832	3.847
2,750	0.42	1.97	3.000	3.406	3.630	3.702	3.181	3.808	3.823
3,000	0.90	2.32	3.103	3.400	3.047	0.742 3.710	3.732	3.760	3.601
3,500	1.40	2.08	3 309	3 581	3 652	3 683	3 700	3 712	3 725
4,000	2.15	3.05	3.438	3.585	3.638	3.658	3.670	3.682	3.694
5,000	2.39	3.15	3.464	3.580	3.619	3.634	3.644	3.656	3.666
6,000	2.67	3.27	3.487	3.560	3.576	3.585	3.592	3.603	3.615
7,000	2.85	3.33	3.488	3.532	3.537	3.544	3.550	3.560	3.569
8,000	2.96	3.35	3.472	3.498	3.503	3.508	3.512	3.520	3.528
9,000	3.03	3.34	3.446	3.469	3.474	3.478	3.482	3.486	3.493
10,000	3.08	3.32	3.411	3.446	3.449	3.452	3.455	3.458	3.461

[°] Values in parentheses represent bubble-point pressures in p.s.i.

^b Partial molal volume in cu. ft./lb.-mole.

of *n*-decane, the partial volume of this less volatile component decreases rapidly. Again, there is a similarity in the behavior of *n*-decane in the ethane-*n*-decane system to the behavior of *n*-pentane in the ethane-*n*-pentane system (4).

The effect of pressure upon the partial volume of ethane in a mixture containing 0.7 mole fraction ethane is shown for each of several temperatures in Figure 3. As expected, the effect of pressure becomes more pronounced at the higher temperatures. Again, the similarity in behavior to ethane in the ethane-*n*-pentane system is evident. Figure 4 depicts the effect of pressure upon the partial volume of *n*-decane for temperatures between 40° and 460° F. The rather anomalous behavior indicated by the rapid decrease in the partial volume at 460° F. with a decrease in pressure is similar to the behavior found for the partial volume of *n*-pentane at temperatures above 280° F. in the ethane-*n*-pentane system (4, 6, 7).

Many more diagrams similar to those presented can be prepared from the information recorded in Tables II and III. However, the foregoing figures illustrate the trends encountered in the partial volumetric behavior of the components of the ethane-n-decane system.

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Figure 2. Influence of composition on the partial molal volume of *n*-decane at 220° F.

NOMENCLATURE

- d = differential operator
- m_k = lb.-moles of component k
- N = number of points
- n_k = mole fraction of component k
- V = molal volume, cu. ft./lb.-mole
- V = partial molal volume, partial volume, cu. ft./lb.-mole
- V = total volume, cu. ft.
- \sum = summation
- σ = standard error of estimate, cu: ft./lb.-mole
- ∂ = partial differential operator

Subscripts

- gr = graphical
- int = integrated
- j, k = components j and k
- m_i = change in state during which the weight of all components other than k remains constant
- P = pressure, p.s.i.a.
- T = thermodynamic temperature, ° R.

Superscript

o = pure component

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Figure 3. Effect of pressure on the partial molal volume of ethane for mixture containing 0.7 mole fraction ethane



Figure 4. Effect of pressure on the partial molal volume of *n*-decane for a mixture containing 0.7 mole fraction *n*-decane

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